

ADVANCED DATA STRUCTURES AND ALGORITHMS

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What this Lecture is about:

- Selection of Data Structure
- General trees
- Binary trees
- Game of questions
- Binary tree terminology
- Converting General Trees To Binary Trees





Selection of Data Structure





There are many considerations to be taken into account when choosing the best data structure for a specific program"

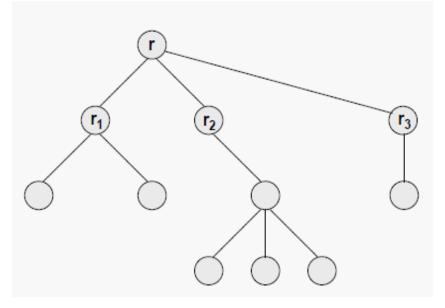
- 1. Size of data.
- 2. Speed and manner data use.
- 3. Data dynamics, as change and edit.
- 4. Size of required storage.
- 5. Fetch time of any information from data structure.



General Trees



A General Tree T is a finite set of one or more nodes such that there is one designated node \mathbf{r} , called the <u>root</u> of \mathbf{T} , and the remaining nodes are partitioned into $\mathbf{n} \geq \mathbf{0}$ disjoint subsets $\mathbf{T1}$, $\mathbf{T2}$, ..., \mathbf{Tn} , each of which is a tree, and whose roots $\mathbf{r1}$, $\mathbf{r2}$, ..., \mathbf{rn} , respectively, are children of \mathbf{r} .

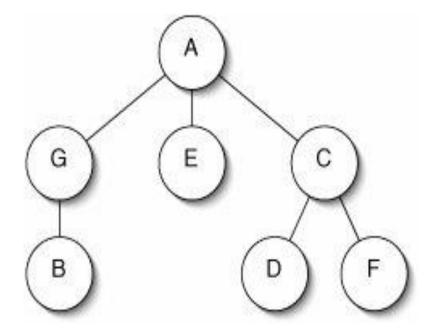




General Trees

A general tree is a tree which each node can have an unlimited child nodes for a given node.

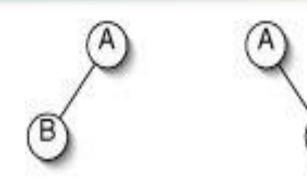
An example of general tree is shown in the following figure: -



A general tree.







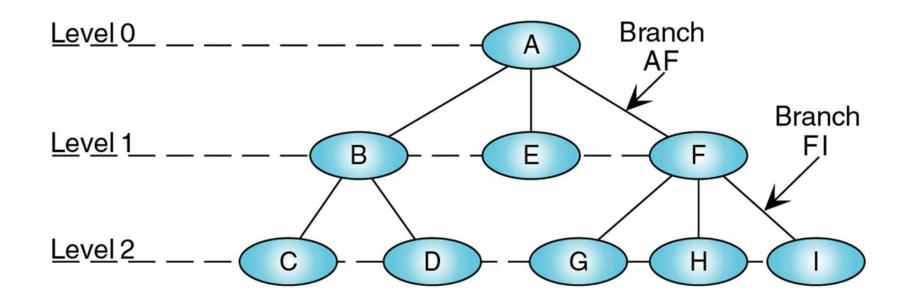


The two binary trees at left are considered different:

- One has an empty right subtree,
- While the other has an empty left subtree,
- Among general trees like the one at right, no such distinction is drawn.
- A general tree cannot be empty. It always has at least one node, but it might not have any subtrees.



General Trees



Parents: A, B, F Children: B, E, F, C, D, G, H, I Siblings: {B,E,F}, {C,D}, {G,H,I}

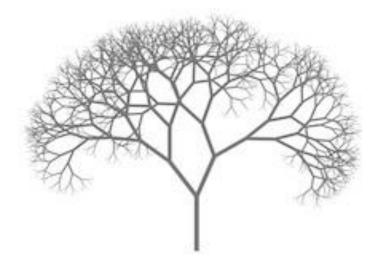
C,D,E,G,H,I Leaves Internal nodes B,F

Binary Trees





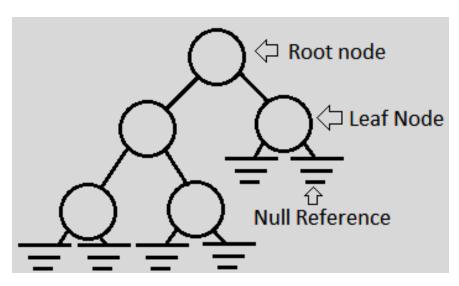
There is a considerable amount of terminology regarding trees. We will introduce it in the context of the game of Questions.





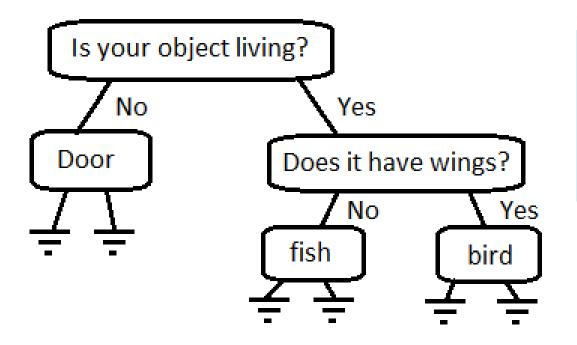
The Game of Questions to Build a Binary Trees

Each node will contain a question and two links to other nodes. If 'yes' is entered for a question, yes Node will be referenced. When the referenced node is a leaf node, the computer will make a guess on the object.





The Game of Questions to Build a Binary Trees



Is your object living?

 $No \rightarrow Door$

Does it have wings?

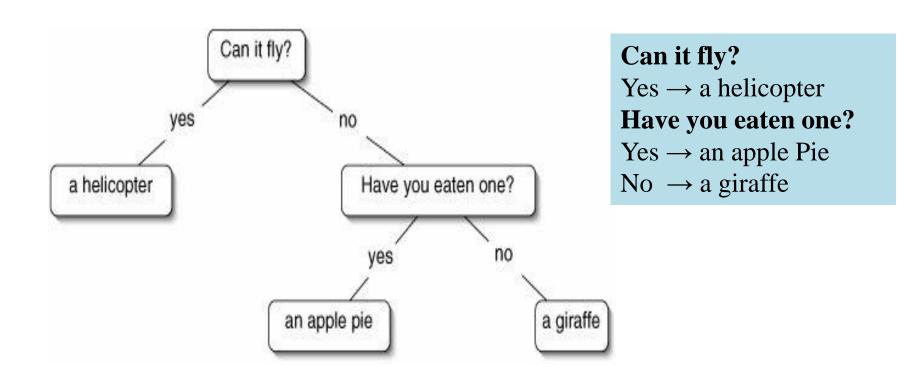
 $No \rightarrow Fish$

 $Yes \rightarrow Bird$



The Game of Questions to Build a Binary Trees

The Game of Questions binary decision tree







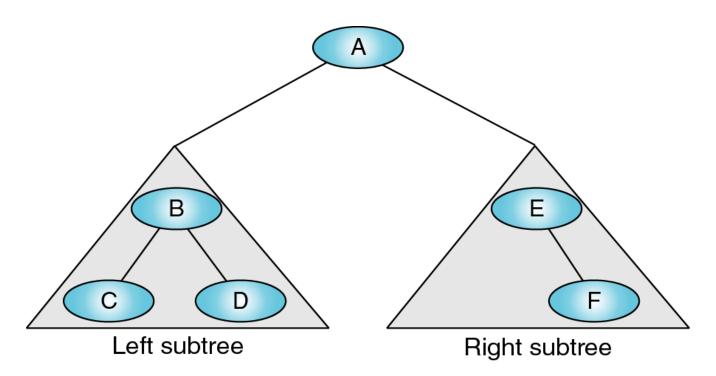
Formally, a binary tree is either:

- A. Empty, or
- B. A node with a left subtree and a right subtree. Each of these subtrees is itself a binary tree.
- C. The most important feature distinguishing binary trees from more general trees is that, in a binary tree, no node can have more than two children.



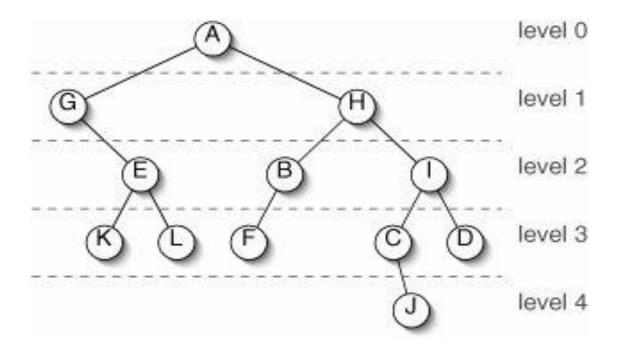


A **binary tree** is a tree in which no node can have more than two subtrees.





More information about some of the nodes is given in the Figure.

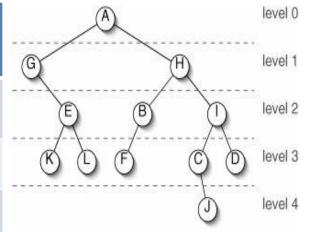


A binary tree with the nodes divided into levels.



Information about some of the nodes of a binary tree with the nodes divided into levels.

Node	Parent	Children	Sibling	Depth
A		G, H		0
В	Н	F	I	2
С	1	J	D	3
D	I		С	3
E	G	K, L		2

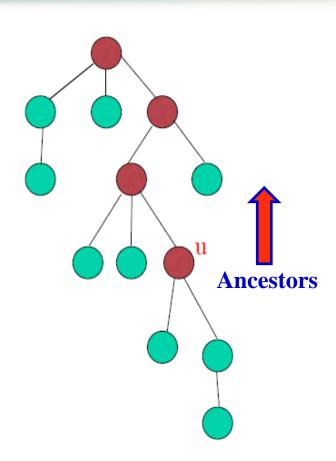




In Figure, the ancestors of L are E, G, and A. A node's proper ancestors are all of its ancestors except itself.

- Siblings: two nodes that have the same parent are called siblings
- Internal nodes
 - nodes that have children
- External nodes or leaves
 - nodes that don't have children
- Ancestors: a node reachable by repeated proceeding <u>from child</u> to parent.
- Descendants: a node reachable by repeated proceeding <u>from</u> <u>parent to child.</u>



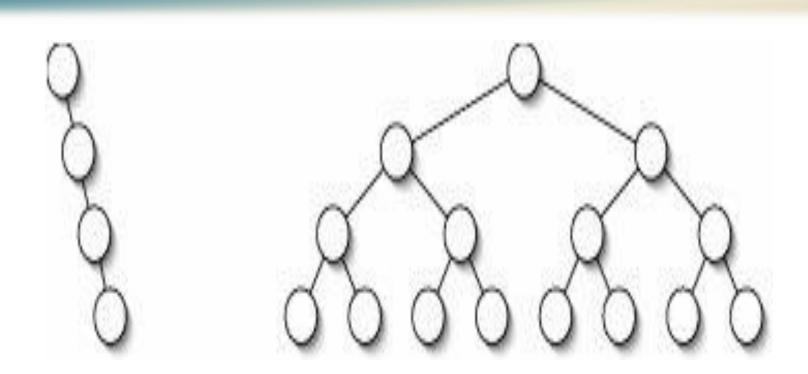


Descendants

Ancestors of u

Descendants of u

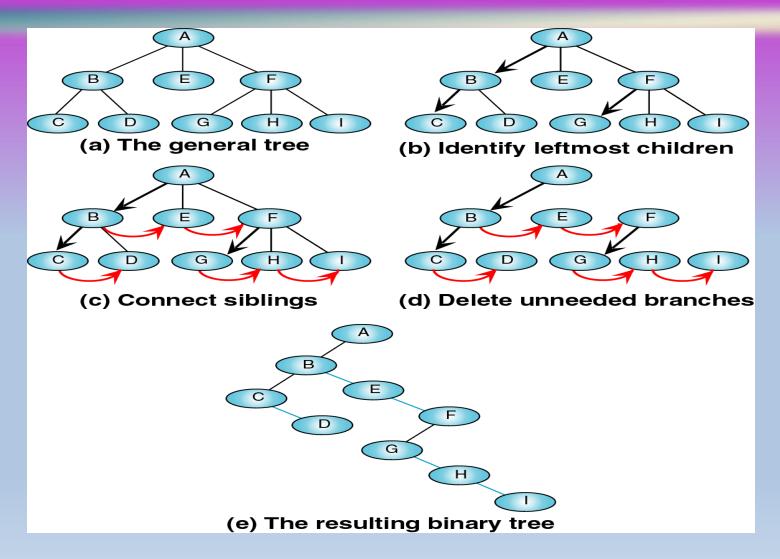




A linear tree (left) and a perfect binary tree (right). Both of these trees are of height 3.



Converting General Trees To Binary Trees



Creating a Binary Tree from a General Tree



